

|              |                                   |
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| <b>S. 70</b> | <b>Varianz einer Zufallsgröße</b> |
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**2 Augensumme**

|              |                |                |                |                |                |                |                |                |                |                |                |
|--------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| Augensumme x | 2              | 3              | 4              | 5              | 6              | 7              | 8              | 9              | 10             | 11             | 12             |
| $P(X = x)$   | $\frac{1}{36}$ | $\frac{2}{36}$ | $\frac{3}{36}$ | $\frac{4}{36}$ | $\frac{5}{36}$ | $\frac{6}{36}$ | $\frac{5}{36}$ | $\frac{4}{36}$ | $\frac{3}{36}$ | $\frac{2}{36}$ | $\frac{1}{36}$ |
|              | 25             | 16             | 9              | 4              | 1              | 0              | 1              | 4              | 9              | 16             | 25             |

$\mu = 7$  und  $\text{Var}(X) = \frac{35}{6}$

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**3 Erwartungswert, Varianz und Standardabweichung**

a)

|               |      |      |      |       |
|---------------|------|------|------|-------|
| x             | -2   | 0    | 2    | 4     |
| $P(X = x)$    | 0,5  | 0,2  | 0,2  | 0,1   |
| $(x - \mu)^2$ | 3,24 | 0,04 | 4,84 | 17,64 |

$E(X) = -0,2$  und  $\text{Var}(X) = 4,36$

b)

|               |      |      |      |      |      |      |
|---------------|------|------|------|------|------|------|
| x             | -3   | -2   | -1   | 0    | 1    | 2    |
| $P(X = x)$    | 0,1  | 0,1  | 0,3  | 0,2  | 0,2  | 0,1  |
| $(x - \mu)^2$ | 6,76 | 2,56 | 0,36 | 0,36 | 1,96 | 5,76 |

$E(X) = -0,4$  und  $\text{Var}(X) = 2,08$

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**4 Satz**

|                   |                |                |               |                |               |               |
|-------------------|----------------|----------------|---------------|----------------|---------------|---------------|
| Wort              | Die            | Varianz        | ist           | eine           | reelle        | Zahl          |
| Wortlänge x       | 3              | 7              | 3             | 4              | 6             | 4             |
| $(x - \mu)^2$     | 2,25           | 6,25           | 2,25          | 0,25           | 2,25          | 0,25          |
| Konsonanzanzahl y | 1              | 4              | 2             | 1              | 3             | 3             |
| $(y - \mu)^2$     | $\frac{16}{9}$ | $\frac{25}{9}$ | $\frac{1}{9}$ | $\frac{16}{9}$ | $\frac{4}{9}$ | $\frac{4}{9}$ |

$E(X) = 4,5$  und  $E(Y) = \frac{7}{3}$

$\text{Var}(X) = 2,25$  und  $\text{Var}(Y) = \frac{37}{27}$

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### 5 Laplace-Münze

|               |               |               |               |
|---------------|---------------|---------------|---------------|
| x             | 1             | 2             | 3             |
| $P(X = x)$    | $\frac{1}{2}$ | $\frac{1}{4}$ | $\frac{1}{4}$ |
| $(x - \mu)^2$ | 0,5625        | 0,0625        | 1,5625        |

$$\text{Var}(X) = 0,6875 \text{ und } E(X) = 1,75$$

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### 6 Treffer und Niete

$$E(X) = 1 \cdot p + 0 \cdot (1 - p) = p$$

und

$$\text{Var}(X) = (1 - p)^2 \cdot p + (0 - p)^2 \cdot (1 - p) = p \cdot (1 - p)(1 - p + p) = p \cdot (1 - p)$$

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### 7 Roulette

$$E(C) = 360 \cdot \frac{1}{37} + 0 \cdot \frac{36}{37} = \frac{360}{37}$$

$$\text{Var}(C) = \left(360 - \frac{360}{37}\right)^2 \cdot \frac{1}{37} + \left(0 - \frac{360}{37}\right)^2 \cdot \frac{36}{37} = 3408,04$$

$$E(H) = 20 \cdot \frac{18}{37} + 0 \cdot \frac{19}{37} = \frac{360}{37}$$

$$\text{Var}(C) = \left(20 - \frac{360}{37}\right)^2 \cdot \frac{18}{37} + \left(0 - \frac{360}{37}\right)^2 \cdot \frac{19}{37} = 99,927$$

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